The notorious Collatz conjecture

Start with any natural number. If it is even, divide it by two. If it is odd, multiply it by three and add one. Repeat this process indefinitely. The Collatz conjecture asserts that no matter how large an initial number is, this process eventually reaches the number one and loops back to one indefinitely after that.